

# Liquidity and Prices in Over-the-Counter Markets with Almost Public Information

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# Motivation

Many assets are traded over-the-counter:

- ▶ residential and commercial real estate
- ▶ private equity
- ▶ derivatives
- ▶ mortgage-backed securities
- ▶ bank loans
- ▶ corporate and municipal bonds
- ▶ sovereign dept

# Motivation

In decentralized markets:

- ▶ search for a counter party takes time (search friction)
- ▶ price is negotiated bilaterally and the negotiation takes time (bargaining friction)

Important to distinguish the bargaining friction:

- ▶ the uncertainty about asset quality operates through negotiation delays
  - ▶ trade delay is a natural screening/signaling device
- ▶ existing literature views the search friction as a reduced form for both frictions
  - ▶ but do they operate similarly?
  - ▶ if not, does it affect policy implications (effect of transparency on the market liquidity)

# This study

A tractable model of liquidity and asset prices in decentralized markets that captures both bargaining and search delays

# This study

The approach is to look at the limit of almost public information (global games approach):

- ▶ agents get very precise signals about the asset quality, but the public information about the quality is crude;
- ▶ negotiation delays still arise, and depend on the amount of public information.

# This study

- ▶ Intensive (negotiation delay) vs extensive (traded or not) trade margins
- ▶ Intensive margin: Liquidity is U-shaped in the asset quality conditional on public info
  - ▶ differs from the adverse selection story (decreasing relation)
- ▶ Extensive margin: Search delays operate differently from bargaining delays
  - ▶ dark and bright side of transparency
- ▶ Asset substitutability
  - ▶ gradual transparency policies hurt market liquidity, flights-to-liquidity
- ▶ Asset price decomposition, clearly separates effect of liquidity premium, market liquidity, and market thickness

## Related Literature

- ▶ **Search-and-bargaining models of OTC markets:** Duffie, Gârleanu, and Pedersen (2005, 2007), Lagos and Rocheteau (2007, 2009), Vayanos and Weill (2008), Weill (2008)
- ▶ **Asset trading with adverse selection:** Guerrieri and Shimer (2014), Chang (2014), Kurlat (2013)
- ▶ **Theoretical search-and-bargaining:** Rubinstein and Wolinsky (1985), Satterthwaite and Shneyerov (2007), Lauer mann and Wolinsky (2014), Atakan and Ekmekci (2014)

# Plan

1. Model
2. Asset and Market Liquidity
3. Flights-to-Liquidity and Transparency
4. Asset Prices
5. Conclusion

# Model

- ▶ Continuum of agents of mass  $a > 1$ .
- ▶ Continuum of asset qualities  $\theta$  in  $[0, 1]$  each in unit supply.
  - ▶ Initially, assets are randomly distributed among agents.
  - ▶ Since  $a > 1$ , not all agents hold an asset.
- ▶ Time is continuous, and agents discount at common rate  $r$ .
- ▶ Two observable types of agents: buyers and sellers.
- ▶ Buyer's flow payoff from asset  $\theta$  is  $k\theta$ .
- ▶ Seller's flow payoff from asset  $\theta$  is  $k\theta - \ell$ .
  - ▶  $k > 0$  is asset heterogeneity.
  - ▶  $\ell > 0$  is holding cost.

# Model

- ▶ Agents are hit by a liquidity shock with Poisson intensity  $y_d$  and recover from it with Poisson intensity  $y_u$ .
- ▶ Shocks and recoveries are independent across agents.
- ▶ Agents are restricted to hold at most one asset.

# Search Stage

- ▶ Agents can trade in the market with the search friction.
- ▶ Matches are independent across agents and time.
- ▶ Buyers of mass  $m_b$  contact sellers of mass  $m_s$  with intensity  $\lambda m_b m_s$ .
  - ▶ **contact intensity  $\lambda$**  reflects the search friction.
  - ▶ smaller  $\lambda \implies$  greater search friction.

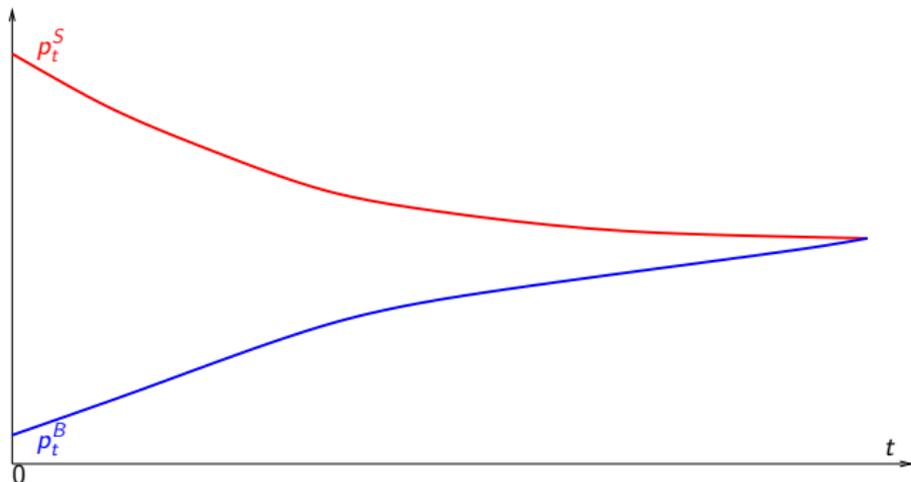
# Bargaining Stage

- ▶ Both sides condition strategies on types and **on the quality  $\theta$** .
  - ▶ interpretation: get noisy private signals about  $\theta$ , look at the limit as the precision goes to  $\infty$ .
- ▶ After the match is found:
  - ▶ all sellers agree to bargain (wlog);
  - ▶ buyers decide whether to proceed to the bargaining stage or continue the search.
- ▶ The strategy of the buyer  $\sigma_\theta \in [0, 1]$  gives the probability with which the buyer participates in the bargaining stage conditional on  $\theta$ .
- ▶ After agents proceed to the bargaining stage:
  - ▶ do not participate in search (prices are only good 'as long as the breath is warm');
  - ▶ only leave the match if one of the types switches or trade occurs (wlog).

# Screening Bargaining Solution

- ▶ The buyer and the seller play the following continuous-time bargaining game.
  - ▶ The buyer makes increasing price offers  $p_t^B$  and the seller makes decreasing price offers  $p_t^S$ .
  - ▶ Bargaining stops when one of the parties accepts the opponent's offer and trade happens at this price.

# Screening Bargaining Solution



**Figure:** The buyer makes continuously increasing offers  $p_t^B$  and the seller makes continuously decreasing offers  $p_t^S$ .

# Screening Bargaining Solution

- ▶ The outcome of the pure-strategy Nash equilibrium of this game can be described by  $(p_\theta, t_\theta)$ .
  - ▶ Outcome  $(p_\theta, t_\theta)$  depends on the choice of price offers  $p_t^B$  and  $p_t^S$ .
  - ▶ Suppose that price paths  $p_t^B$  and  $p_t^S$  are chosen so that in equilibrium,  $p_\theta$  splits trade surplus between the buyer and the seller in proportion  $\alpha$  and  $1 - \alpha$  where  $\alpha \in (0, 1)$ .
  - ▶ This pins down uniquely  $t_\theta$ . Call this outcome  $(p_\theta, t_\theta)$  SBS.

# Microfoundations

- ▶ Microfoundation (Tsoy, 2015):
  - ▶ agents get noisy private signals about asset quality that determine their values (global games information structure)
  - ▶ agents alternate making price offers (as in Rubinstein, 1982)
- ▶ The SBS outcome is the limit of a sequence of equilibria in the bargaining game as the noise goes to zero and offers become frequent
- ▶ Why delay?
  - ▶ Despite precise signals, the public information about the quality is crude
  - ▶ Public info determines the bargaining delays

Details

# Equilibrium

- ▶  $M$  is the distribution of assets among agents

## Definition

A tuple  $(\sigma_\theta, M)$  constitutes an **equilibrium** if

- ▶ the buyer's strategy  $\sigma_\theta$  is optimal given  $M$ ,
- ▶  $M$  is the steady-state distribution of assets generated by  $\sigma_\theta$ .

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# Intensive Margin: U-shaped Liquidity

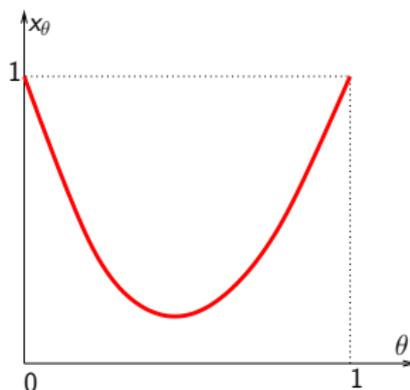
- ▶ **Liquidity** of asset  $\theta$  – real costs of trade delay  $t_\theta$ :

$$x_\theta \equiv e^{-\rho t_\theta}, \text{ where } \rho \equiv r + y_u + y_d.$$

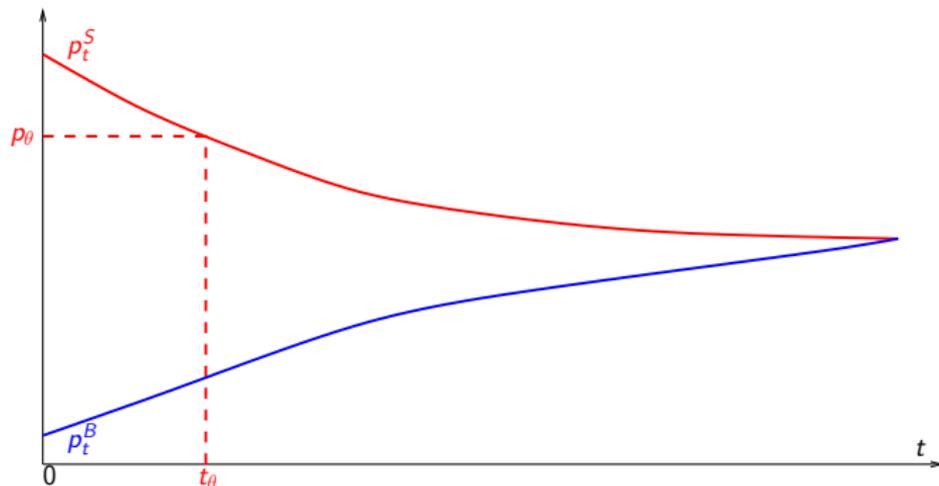
- ▶ In equilibrium,  $x_\theta$  is an increasing function of an asset turnover ( $x_\theta \approx \text{turnover}$  when  $r$  is small relative to  $y_u + y_d$ ).

## Theorem

*Liquidity  $x_\theta$  is U-shaped in quality  $\theta$ .*

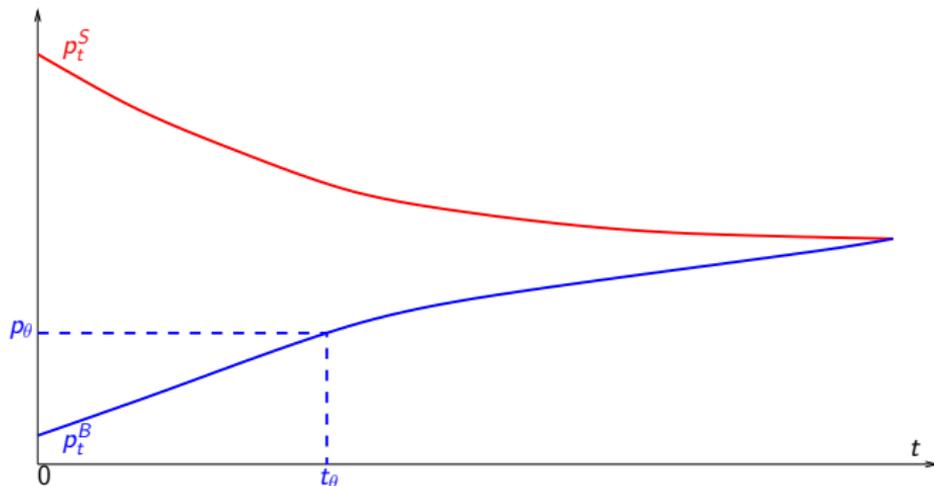


# Intensive Margin: U-shaped Liquidity



**Figure:** For relatively **high** asset qualities, the **buyer** of asset  $\theta$  prefers to accept price offer of the seller  $p_\theta$  at time  $t_\theta$  rather than any other price offer.

# Intensive Margin: U-shaped Liquidity



**Figure:** For relatively **low** asset qualities, the **seller** of asset  $\theta$  prefers to accept price offer of the buyer  $p_\theta$  at time  $t_\theta$  rather than any other price offer.

# Intensive Margin: U-shaped Liquidity

- ▶ In contrast to the decreasing relationship in adverse selection models (e.g. Guerrieri and Shimer, 2014).
  - ▶ primary markets: adverse selection (asym info b/w originator and buyers).
  - ▶ secondary markets: both sides have private information.

# Extensive Margin: Shopping for Liquidity

- ▶ **Intensive margin:** asset liquidity  $x_\theta$
- ▶ **Extensive margin**
  - ▶ **Liquid assets:**  $\theta \in \Theta_L \iff \sigma_\theta = 1$
  - ▶ **Illiquid assets:**  $\theta \in \Theta_I \iff \sigma_\theta = 0$
- ▶ **Market thickness:**  $\Lambda_s$  and  $\Lambda_b$  equilibrium intensities of contact for sellers and buyers, resp.
- ▶ **Average liquidity:**

$$\bar{x} \equiv \mathbb{E}[x_\theta | \theta \in \Theta_L]$$

## Theorem

*In equilibrium, there is a threshold  $\underline{x} \equiv \frac{\Lambda_b}{\rho + \Lambda_b} \bar{x}$  such that*

$$x_\theta > \underline{x} \implies \theta \in \Theta_L,$$

$$x_\theta < \underline{x} \implies \theta \in \Theta_I.$$

# Extensive Margin: Shopping for Liquidity

- ▶ Buyers have the outside option of finding another asset in the market  $\implies$  shop for the most liquid assets
  - ▶ non-trivial search in equilibrium
- ▶ Asset qualities in the middle of the distribution may be rejected by buyers

## Theorem

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# Extensive Margin: Shopping for Liquidity

- ▶ Even when observable search and negotiation delays are relatively short (e.g. corp. bonds), does not mean they don't matter:
  - ▶ extensive margin leads to illiquidity of assets

## Theorem

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# Bargaining vs Search Friction

Define **market liquidity**  $L \equiv |\Theta_L|$  to be the mass of assets accepted by buyers ( $\sigma_\theta = 1$ ).

## Theorem

*Market liquidity  $L$  is*

- ▶ *decreasing in the **asset heterogeneity**  $k$ ,*
- ▶ *decreasing in the **contact intensity**  $\lambda$ .*

*Average liquidity  $\bar{x}$  is decreasing in  $k$  and increasing in  $\lambda$ .*

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The severity of the bargaining friction is linked to  $k$ .

- ▶ If there is no difference in payoffs ( $k = 0$ ), then there is no bargaining delays.
- ▶ Higher differences in payoffs ( $\uparrow k$ )  $\implies$  the highest and the lowest price offers are farther apart  $\implies$  trade delays higher ( $\uparrow t_\theta$ )  $\implies$  buyers are willing to accept fewer assets ( $\downarrow L$ ).

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Difference between Treasuries and housing markets.

- ▶ Greater heterogeneity conditional on public information  $\implies$  longer negotiation delays.

Liquidity during periods of heightened market uncertainty.

- ▶ Public information (e.g. credit ratings) becomes less accurate  $\implies$  less liquid markets.

# Bargaining Friction ( $k$ )

$y_u$	$y_d$	$\lambda$	$r(\%)$	$\alpha$	$a$	$k$	$\ell$
70	.2	1500	12	.7	1.5	.01	4

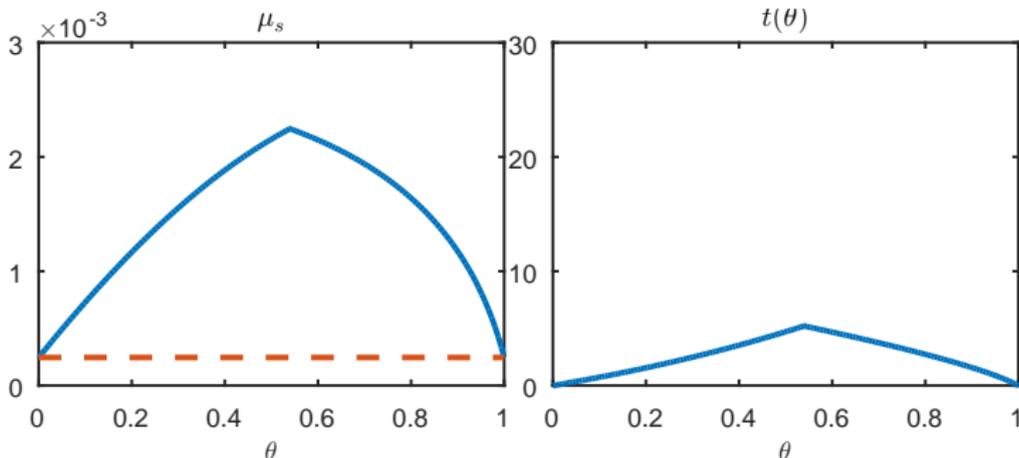


Figure: Mass of sellers holding asset quality  $\theta$  and delay  $t_\theta$ .

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70	.2	1500	12	.7	1.5	.04	4

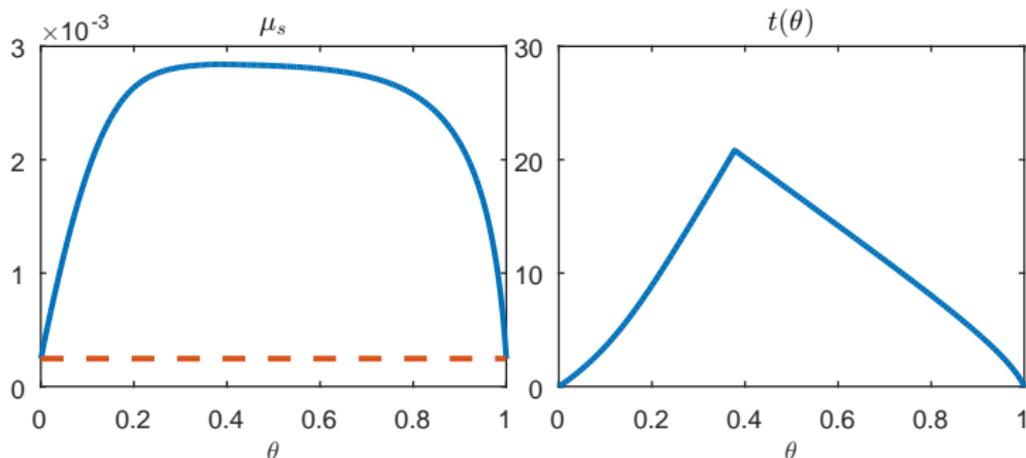


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# Bargaining Friction ( $k$ )

$y_u$	$y_d$	$\lambda$	$r(\%)$	$\alpha$	$a$	$k$	$\ell$
70	.2	1500	12	.7	1.5	.06	4

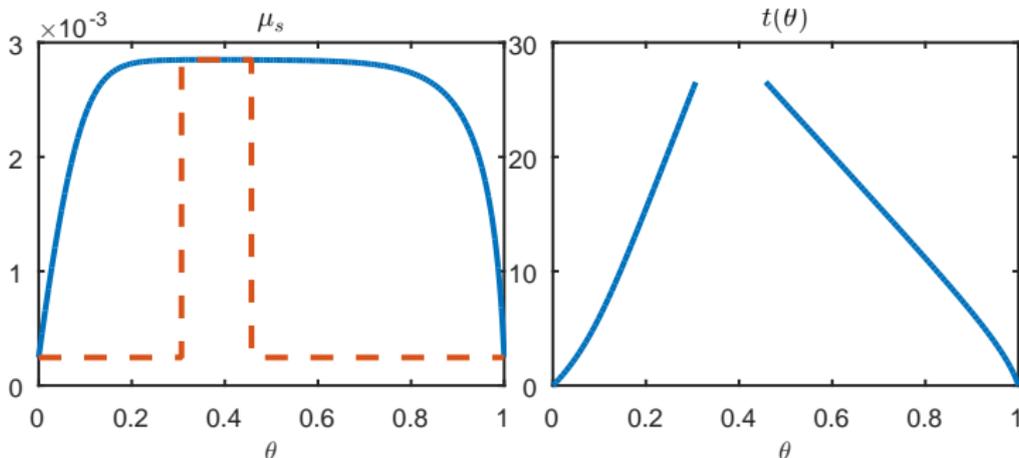


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## Search Friction ( $\lambda$ )

Define **market liquidity**  $L \equiv |\Theta_L|$  to be the mass of assets accepted by buyers ( $\sigma_\theta = 1$ ).

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*Average liquidity  $\bar{x}$  is decreasing in  $k$  and increasing in  $\lambda$ .*

- ▶ The search friction increases the market liquidity  $L$ .
  - ▶ Harder to find a counter-party ( $\downarrow \lambda$ )  $\implies$  buyers' outside option of continuing search decreases  $\implies$  buyers are willing to accept a wider range of assets for trade ( $\uparrow L$ ).

# Search Friction ( $\lambda$ )

$y_u$	$y_d$	$\lambda$	$r(\%)$	$\alpha$	$a$	$k$	$\ell$
70	.2	1500	12	.7	1.5	.06	4

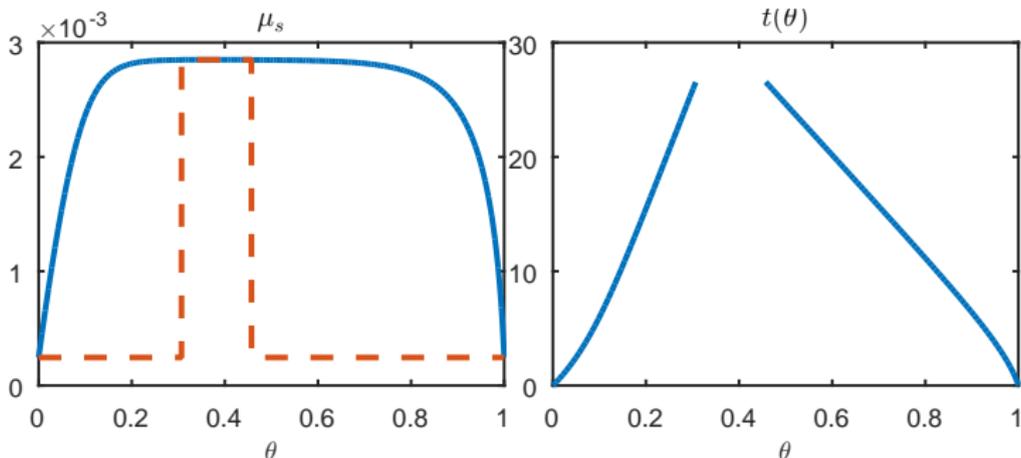


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# Search Friction ( $\lambda$ )

$y_u$	$y_d$	$\lambda$	$r(\%)$	$\alpha$	$a$	$k$	$\ell$
70	.2	100	12	.7	1.5	.06	4

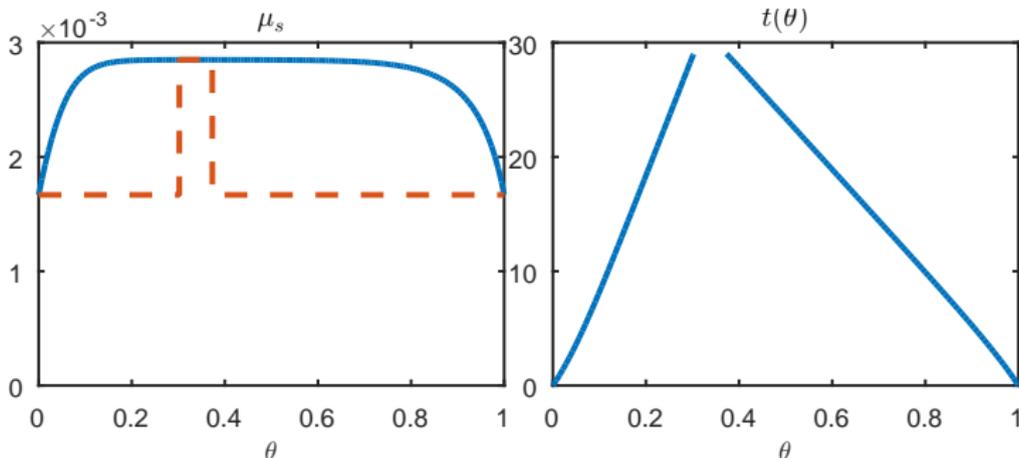


Figure: Mass of sellers holding asset quality  $\theta$  and delay  $t_\theta$  .

# Bright and Dark Sides of Transparency

- ▶ Bright side:  $\uparrow$ transparency (credit ratings, benchmarks, quotes)  $\implies$   $\uparrow$ public info  $\implies$   $\downarrow$ bargaining friction  $\implies$   $\uparrow$ market liquidity
- ▶ Dark side:  $\uparrow$ transparency (trading platform, post-trade)  $\implies$   $\downarrow$ search friction  $\implies$   $\downarrow$ market liquidity
  - ▶ Transparency ( $\uparrow \lambda$ ) increases the aggregate welfare through shorter search times, but this is not a Pareto-improvement
  - ▶ Fewer assets are actively traded ( $\downarrow L$ ) and owners of assets that become illiquid are worse off

# Plan

1. Model.
2. Asset and Market Liquidity.
3. Flights-to-Liquidity and Transparency.
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# Flights and Transparency

## Theorem

*Market liquidity  $L$  is increasing in the mass of agents  $a$ .*

- ▶ Two asset classes indexed by  $i = 1, 2$  each of mass 1, a mass  $a > 2$  of agents.
- ▶ For each class  $i$ , flow payoffs of the buyer and seller are parametrized by  $k_i$ .
- ▶ The mass  $a_i \geq 1$  of agents trading assets in each class  $i$  is determined in equilibrium so that  $a_1 + a_2 = a$ .

## Definition

*A tuple  $(\sigma_\theta^i, M^i, a_i)_{i=1,2}$  is a **multi-class equilibrium** if  $(\sigma_\theta^i, M^i)$  is the equilibrium of the baseline model with mass of agents  $a_i$  and the following condition holds*

$$\begin{cases} \underline{x}^1 = \underline{x}^2, & \text{if } a - 1 > a_1 > 1, \\ \underline{x}^1 \leq \underline{x}^2, & \text{if } a_1 = 1, \\ \underline{x}^1 \geq \underline{x}^2, & \text{if } a_1 = a - 1. \end{cases}$$

# Flights-to-Liquidity

- ▶ Consider a model with two classes: class 1 ( $k_1 > 0$ ) and class 2 ( $k_2 = 0$ ).
  - ▶ AAA securities and Treasuries: flights-to-liquidity exacerbate drop in liquidity from the increase in the bargaining friction
  - ▶ High-yield and investment-grade bonds: post-trade transparency was introduced gradually at first covering only investment-grade bonds  $\implies$  hurt liquidity of high yield bonds (Asquith et al., 2013)

## Theorem

*Suppose the range of asset payoffs  $k_1$  in class 1 increases to  $\tilde{k}_1$ . Then the set of liquid assets in class 1 decreases to  $\tilde{L}_1 < L_1$  and agents migrate from trading assets in class 1 to trading assets in class 2 ( $a_1 < \tilde{a}_1$  and  $a_2 > \tilde{a}_2$ ).*

# Flights-to-Liquidity

$y_u$	$y_d$	$\lambda$	$r(\%)$	$\alpha$	$a$	$k$	$\ell$	$a_1$
70	.2	1500	12	.7	3.52	.01	4	1.49

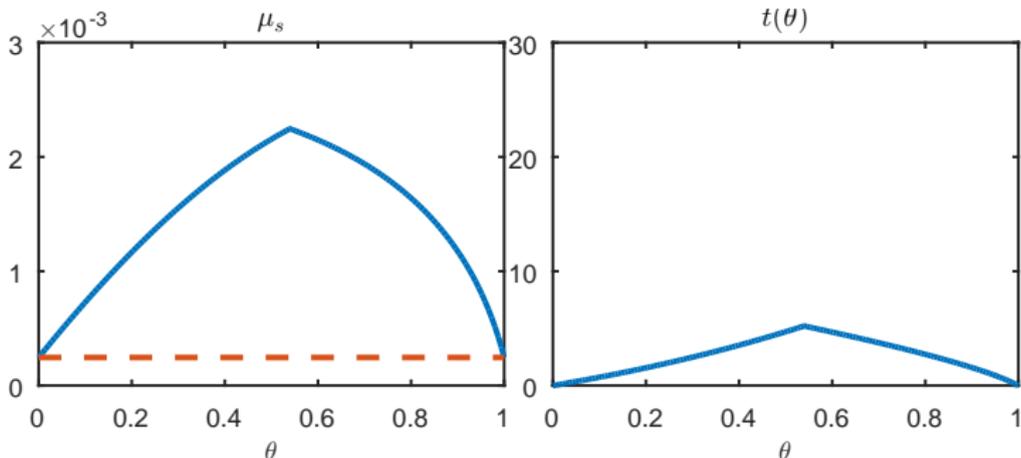


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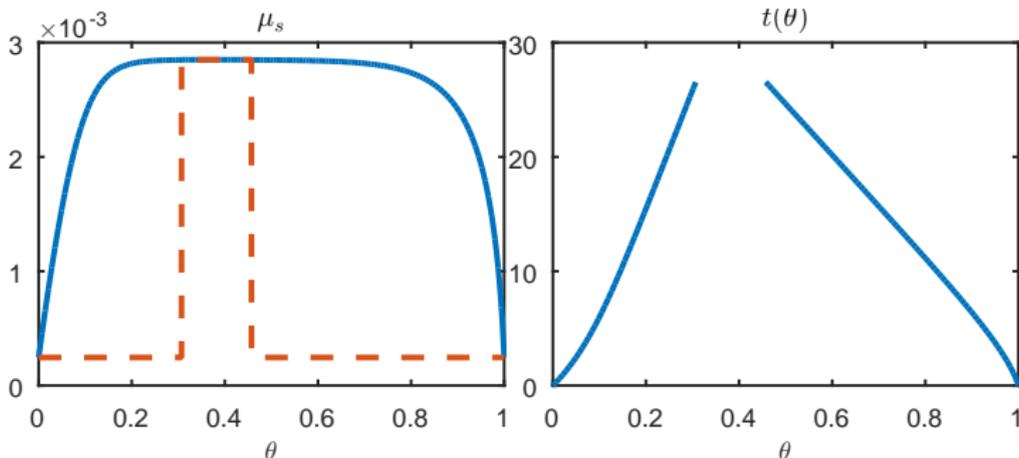


Figure: Mass of sellers holding asset quality  $\theta$  and liquidity  $t_\theta$ .

# Flights-to-Liquidity

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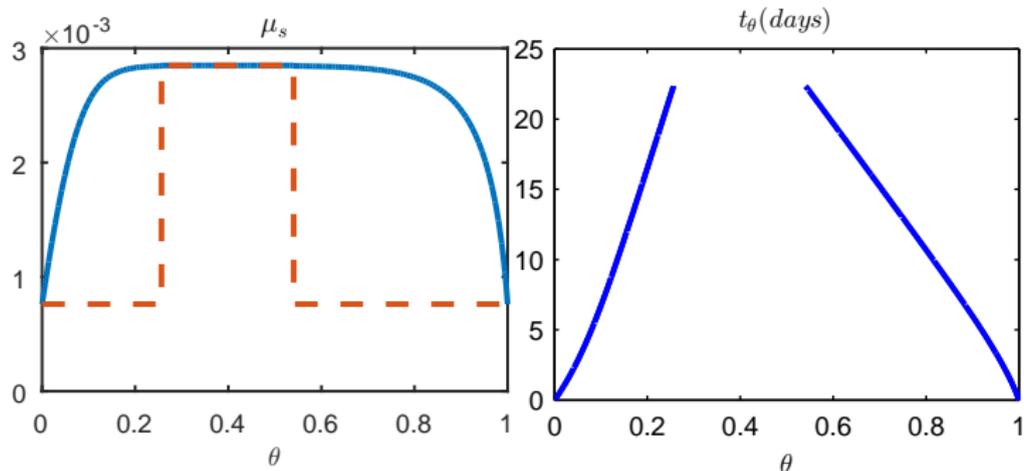


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Conclusion

# Asset Price Decomposition

## Theorem

*In equilibrium, prices of assets in  $\Theta_L$  are given by*

$$p_\theta = \frac{1}{r} \left( k\theta - \frac{r + y_d}{r + y_d + y_u} \ell \right) + (1 - \alpha) \frac{\ell}{\rho} + (1 - \alpha) \frac{y_d}{r} \frac{\Lambda_s}{\rho + \Lambda_s} \frac{\ell}{\rho} x_\theta - \alpha \frac{\ell}{\rho} \frac{y_u}{r} \frac{\Lambda_b}{\rho + \Lambda_b} \bar{x}.$$

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- ▶ Fundamental-value = price if there were no market:
  - ▶ NPV of flow payoffs + surplus from trade to the seller.
- ▶ Higher quality ( $\uparrow \theta$ )  $\implies$  less costly to keep the asset during the search  $\implies \uparrow$  seller's outside option  $\implies \uparrow p_\theta$ .

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▶ Liquidity-premium component:

- ▶ more liquid asset ( $\uparrow x_\theta$ )  $\implies$  conditional on finding a partner, the seller realizes gains from trade more quickly  $\implies \uparrow$  seller's outside option  $\implies \uparrow p_\theta$ .

▶ Average-liquidity component:

- ▶ higher average liquidity ( $\uparrow \bar{x}$ )  $\implies$  conditional on finding a partner, the buyer is more likely to be matched to a seller of a more liquid asset  $\implies \uparrow$  buyer's outside option  $\implies \downarrow p_\theta$ .

# Asset Price Decomposition

## Theorem

In equilibrium, prices of assets in  $\Theta_L$  are given by

$$p_\theta = \frac{1}{r} \left( k\theta - \frac{r + y_d}{r + y_d + y_u} \ell \right) + (1 - \alpha) \frac{\ell}{\rho} + \underbrace{(1 - \alpha) \frac{y_d}{r} \frac{\Lambda_s}{\rho + \Lambda_s \rho} \ell}_{\text{liquidity premium}} x_\theta - \underbrace{\alpha \frac{y_u}{r} \frac{\Lambda_b}{\rho + \Lambda_b \rho} \ell}_{\text{average liquidity}} \bar{x}.$$

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## Theorem

In equilibrium, prices of assets in  $\Theta_L$  are given by

$$p_\theta = \frac{1}{r} \left( k\theta - \frac{r + y_d}{r + y_d + y_u} \ell \right) + (1-\alpha) \frac{\ell}{\rho} + \underbrace{(1-\alpha) \frac{y_d}{r} \frac{\Lambda_s}{\rho + \Lambda_s} \frac{\ell}{\rho} x_\theta}_{\text{liquidity premium}} - \underbrace{\alpha \frac{y_u}{r} \frac{\Lambda_b}{\rho + \Lambda_b} \frac{\ell}{\rho} \bar{x}}_{\text{average liquidity}}.$$

- ▶ Market thickness measures ( $\Lambda_s$  and  $\Lambda_b$ ) affect the sensitivity of price to liquidity and average-liquidity.
  - ▶ liquidity/average liquidity affect outside options only after agents find partners.

# Asset Price Decomposition

## Theorem

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- ▶ DGP ( $x_\theta = \bar{x} = 1$ ) already have a liquidity component but its sign is ambiguous.
- ▶ The bargaining friction allows for further decomposition into non-ambiguous liquidity premium and average-liquidity components.

# Asset Price Decomposition

## Theorem

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- ▶ Longstaff, Mithal, Neis (2005) shows empirically that
  - ▶ corporate spreads can be decomposed into default and non-default components;
  - ▶ non-default component
    - ▶ varies with liquidity measures in the cross-section of assets (liquidity-premium component);
    - ▶ and depends on the market-wide liquidity in the time series analysis (average-liquidity component).

# Conclusion

Tractable model of liquidity in OTC markets arising from negotiation delays.

- ▶ Intensive margin: U-shaped dependence of liquidity on asset quality conditional on public information.
- ▶ Extensive margin: bargaining and search frictions operate differently.
- ▶ Bright and dark side of transparency, credit ratings, and emergence of flights-to-liquidity.
- ▶ Asset price decomposition.

Directions for future research.

- ▶ U-shaped liquidity pattern is testable.
- ▶ Framework can accommodate various forms of asset-specific trade delay.
- ▶ The role of dealers that face bargaining friction.

# Microfoundation for SBS

Sequential bargaining model with private correlated values.

- ▶ The buyer gets a signal  $\theta_b$  about the quality and the seller gets a signal  $\theta_s$  about the quality.

$$\begin{aligned}\theta_b &= \theta + \varepsilon_b, \\ \theta_s &= \theta + \varepsilon_s,\end{aligned}$$

where  $\theta$  is distributed on  $[0, 1]$  and  $\varepsilon_b, \varepsilon_s$  are conditionally independent with bounded support in  $[\theta - \frac{\eta}{2}, \theta + \frac{\eta}{2}] \cap [0, 1]$ .

- ▶ The buyer's value is  $v(\theta_b)$  and the seller's cost is  $c(\theta_s)$ , where  $v$  and  $c$  are strictly increasing functions.
- ▶ Players alternate making offers with the interval between offers  $\Delta$ .
- ▶ Consider continuous-time limits of PBEs, i.e.  $\Delta \rightarrow 0$ .

# Microfoundation for SBS

Consider continuous-time limits of equilibrium with two-sided screening dynamics, i.e.

- ▶ the buyer makes increasing offers irrespective of type,
- ▶ the seller makes decreasing offers irrespective of types,
- ▶ both sides gradually accept offers of each other.

Tsoy (2015) shows:

- ▶ For any  $\eta$ , there is a variety of continuous-time limits of equilibrium with two-sided screening dynamics.
- ▶ Under the support restriction on beliefs, the unique two-sided screening dynamics coinciding with SBS is selected as  $\eta \rightarrow 0$ .

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